

**PHYSICS****ELECTROSTATICS**

41. (3)

Charge density,  $\sigma = \frac{\text{charge}}{\text{area}}$

When two conductors are connected by a conducting wire, then they have same potential i.e.,  $V_1 = V_2$

$$\therefore \frac{1}{4\pi\epsilon_0} \frac{Q_1}{R_1} = \frac{1}{4\pi\epsilon_0} \frac{Q_2}{R_2}$$

$$\Rightarrow \frac{1}{4\pi\epsilon_0} \frac{Q_1}{R_1} \times \frac{R_1}{R_1} = \frac{1}{4\pi\epsilon_0} \frac{Q_2}{R_2} \times \frac{R_2}{R_2}$$

$$\Rightarrow \frac{Q_1 R_1}{4\pi R_1^2} = \frac{Q_2 R_2}{4\pi R_2^2 \epsilon_0}$$

$$\therefore \frac{4\pi R_1^2}{Q_2} = \frac{R_2}{R_1} \text{ or } \frac{\sigma_1}{\sigma_2} = \frac{R_2}{R_1}$$

42. (1)

Let charge and radius of smaller drop is  $q$  and  $r$  respectively and  $R$  = radius of bigger drop

For smaller drop, electric potential,

$$V = \frac{kq}{r} = 220 \text{ V}$$

As volume remains the same

$$\left(\frac{4}{3}\pi r^3\right) \times 27 = \frac{4}{3}\pi R^3$$

$$\Rightarrow R = \sqrt[3]{27r} = 3r$$

And from conservation of charge  $Q = 27q$

$\therefore$  Potential of bigger drop,

$$V_{\text{big drop}} = \frac{kQ}{R} = \frac{k(27q)}{3r} = 9\left(\frac{kq}{r}\right) = 9 \times 220 = 1980 \text{ V}$$

43. (1)

Potential in a region is given by

$$V = 6xy - y + 2yz$$

As we know the relation between electric potential and electric field is

$$\vec{E} = -\left(\frac{\partial V}{\partial x}\hat{i} + \frac{\partial V}{\partial y}\hat{j} + \frac{\partial V}{\partial z}\hat{k}\right)$$

where  $V = 6xy - y + 2yz$

$$\vec{E} = -\left[(6y\hat{i} + (6x - 1 + 2z)\hat{j} + (2y)\hat{k}\right]$$

$$\vec{E}_{(1,1,0)} = -\left(6\hat{i} + 5\hat{j} + 2\hat{k}\right)$$

44. (3)

Potential energy of electric dipole in external electric field.

$$U = -\vec{P} \cdot \vec{E} = -PE \cos \theta = -PE \cos 180^\circ$$

Single angle between  $\vec{E}$  and  $\vec{P}$  is  $180^\circ$

$$\therefore U = +PE$$

On moving towards right electric field strength decrease

$\therefore U$  decreases.

Net force on electric dipole is towards right and net torque acting on it is zero so move towards right.

45. (4)

46. (3)

$$\text{Series: } C_1 = \frac{C}{2}$$

$$\text{Parallel: } C_2 = 2C$$

$$\frac{C_1}{C_2} = \frac{C}{2} = 1:4$$

47. (2)

Energy stored in the system initially

$$U_i = \frac{1}{2}CE^2$$

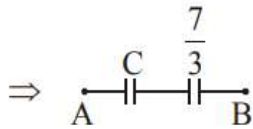
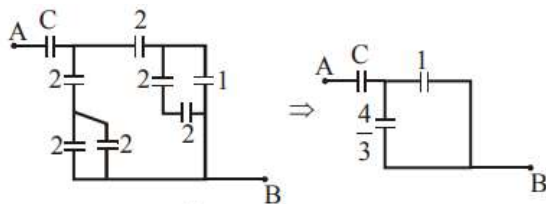
$$U_f = \frac{1}{2} \frac{Q^2}{C_{\text{eq}}} = \frac{(CE)^2}{2 \times 4C} = \frac{1}{2} \frac{CE^2}{4}$$

[As  $Q = CE$  and  $C_{\text{eq}} = 4C$ ]

$$\Delta U = \frac{1}{2}CE^2 \times \frac{3}{4} = \frac{3}{8}CE^2 = \frac{3}{8} \frac{Q^2}{C}$$

48. (1)

From series combination

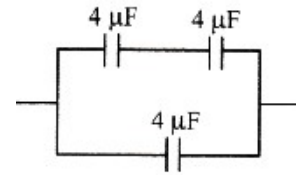


$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} \Rightarrow \frac{1}{\frac{7C}{3}} = \frac{1}{C} + \frac{1}{\frac{4}{3}}$$

$$\Rightarrow 14C = 7 + 3C \Rightarrow C = \frac{7}{11} \mu\text{F}$$

49. (4)

To get effective capacitance of  $6 \mu\text{F}$  two capacitors of  $4 \mu\text{F}$  each connected in series and one of  $4 \mu\text{F}$  capacitor in parallel with them.



Two capacitances in series

$$\therefore \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$$

1 capacitor in parallel

$$\therefore C_{eq} = C_3 + C = 4 + 2 = 6 \mu\text{F}$$

50. (2)

As  $n$  plates are joined alternately positive plate of all  $(n - 1)$  capacitor are connected to one point and negative plate of all  $(n - 1)$  capacitors are connected to other point.

It means  $(n-1)$  capacitors joined in parallel. Therefore, resultant capacitance =  $(n - 1)C$